

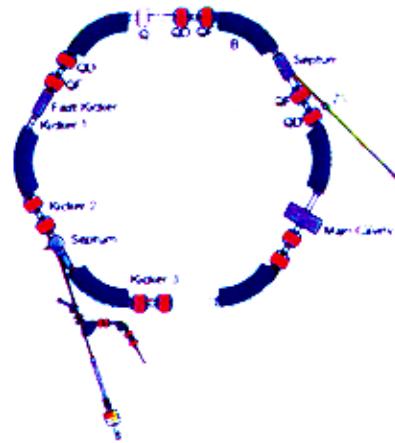
# BEAM-BASED ALIGNMENT OF A HELICAL UNDULATOR

Hiroyuki Hama

with UVSOR Machine & FEL Group  
(Masahito Hosaka, Shigeru Kouda, Jun-Ichiro Yamazaki)

*UVSOR Facility, Institute for Molecular Science, Myodaiji, Okazaki 444 Japan*

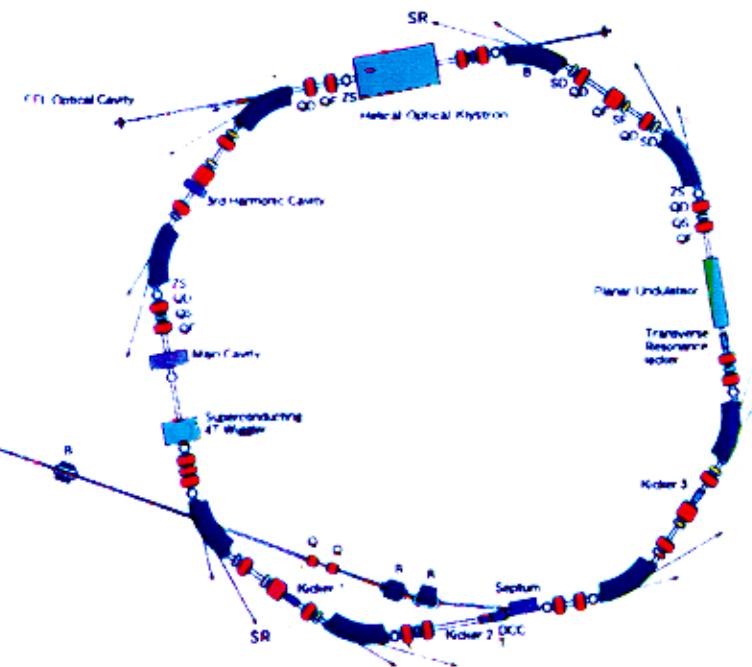
## 600 MeV Booster Synchrotron



## 15 MeV Injector Linac

Beam Transport

## 750 MeV Storage Ring



The UVSOR Accelerator Complex



## Insertion Devices

## Superconducting Wiggler

Wiggler type	Wavelength shifter
Number of poles	3
Magnetic field	4 T max.
Critical energy	1.5 keV @ 750 MeV
Planar Undulator	
Number of periods	24
Period length	8.4 cm
Total length	201.6 cm
Remanent field	0.9 T
Available gap	30 - 90 mm
Deflection parameter K	0.6 - 3.6
1st harm. photon energy	8 - 52 eV @ 750 MeV

## Helical Optical Klystron Undulator (for FEL)

Number of periods	18 (9 × 2)
Period length	11 cm
Length of buncher	33 cm
Total Length	235.12 cm
Remanent field	1.3 T
Available gap	30 - 150 mm
Deflection parameter K	0.07 - 4.6 (Helical mode) 0.15 - 8.5 (Planar mode)
1st harm. photon energy	2 - 45 eV @ 750 MeV (Helical mode)

# Helical Optical Klystron "UNKO-3"

Magnet

NEOMAX44H

B<sub>r</sub>

1.3 T

Length

2350 mm

l<sub>0</sub>

110 mm

Number of Periods

9 + 9

Length of Dispersive section

330 mm

Minimum gap

30 mm

$\lambda = 11 \text{ cm}$

9 periods

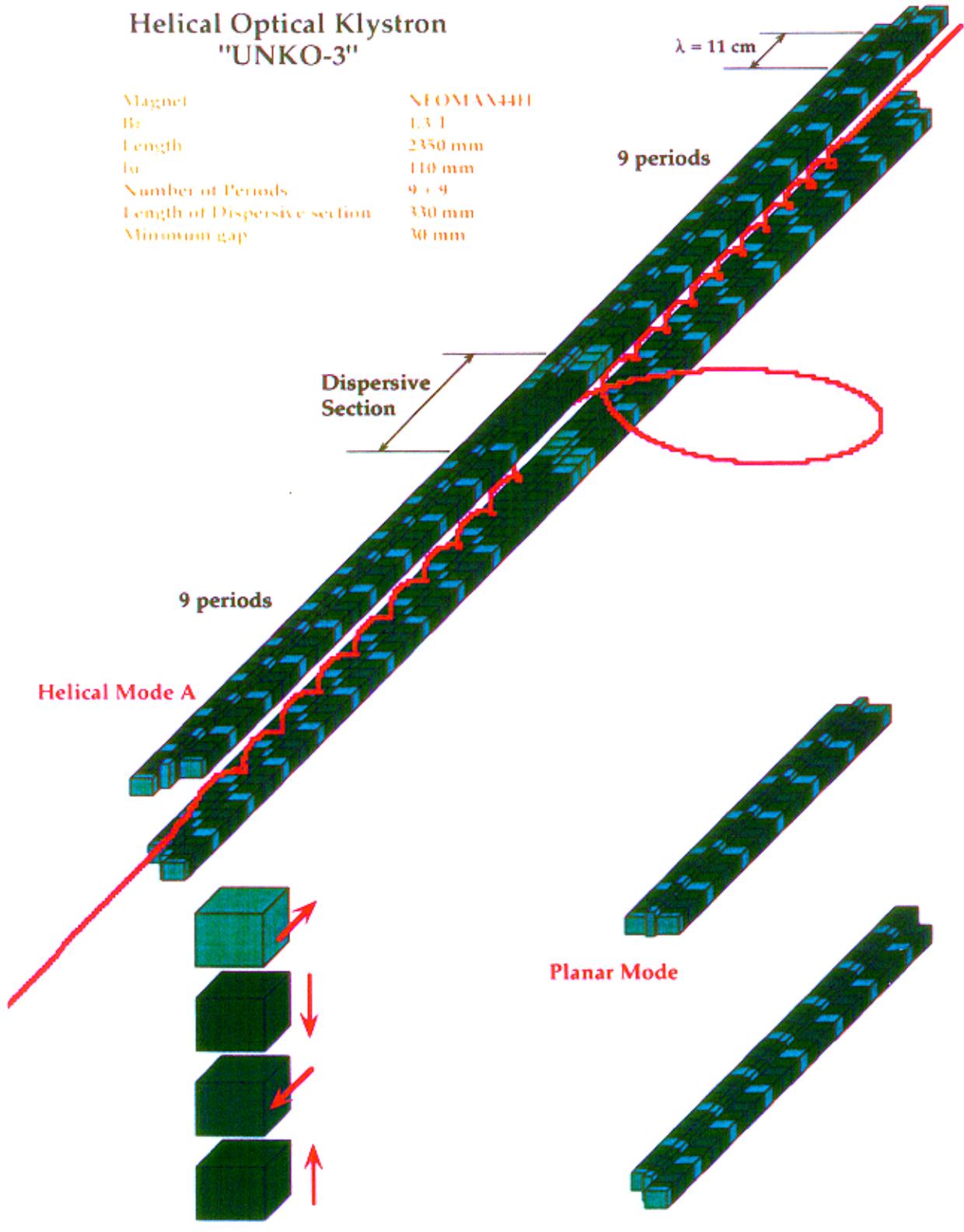
Dispersive  
Section

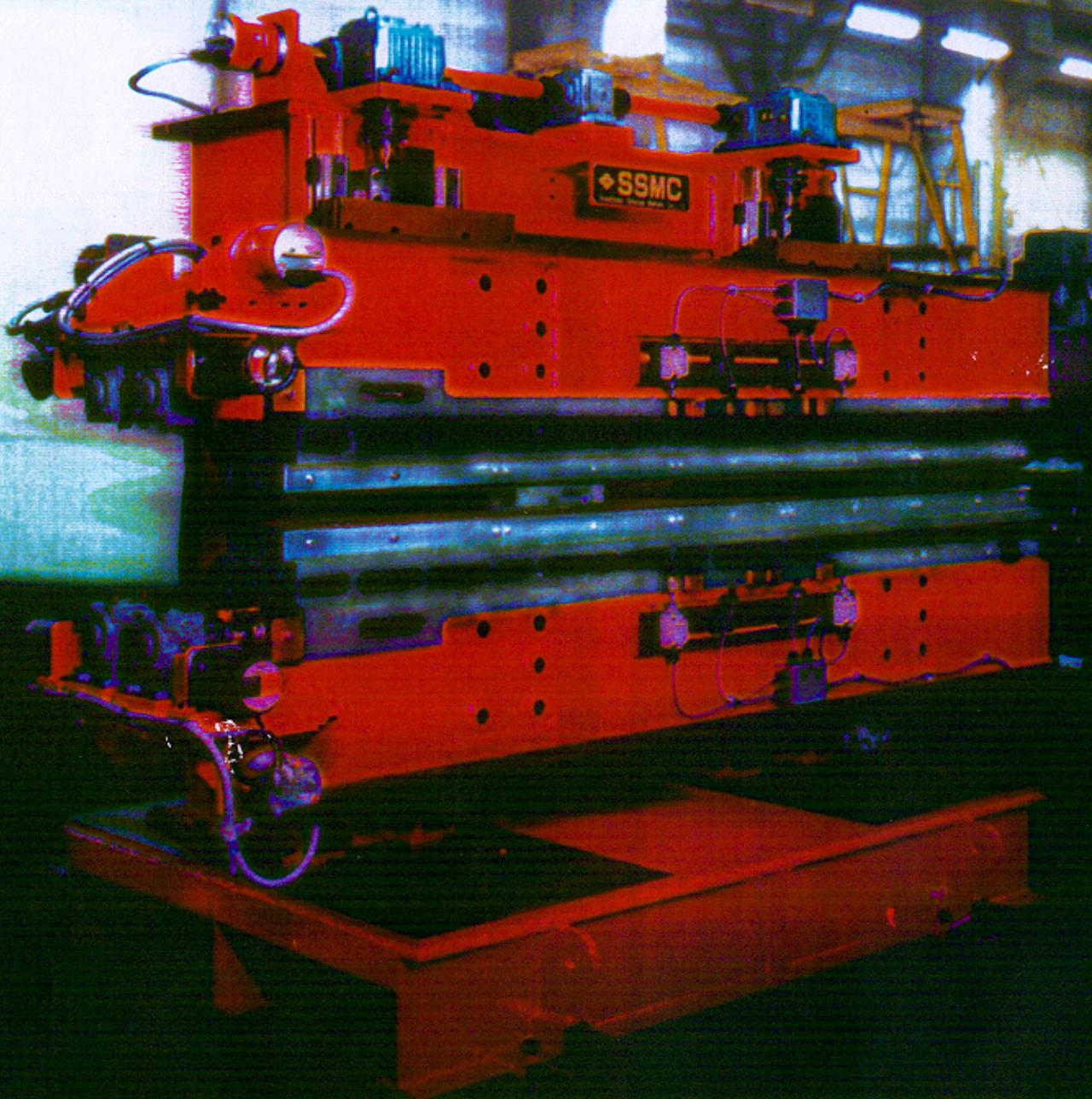
9 periods

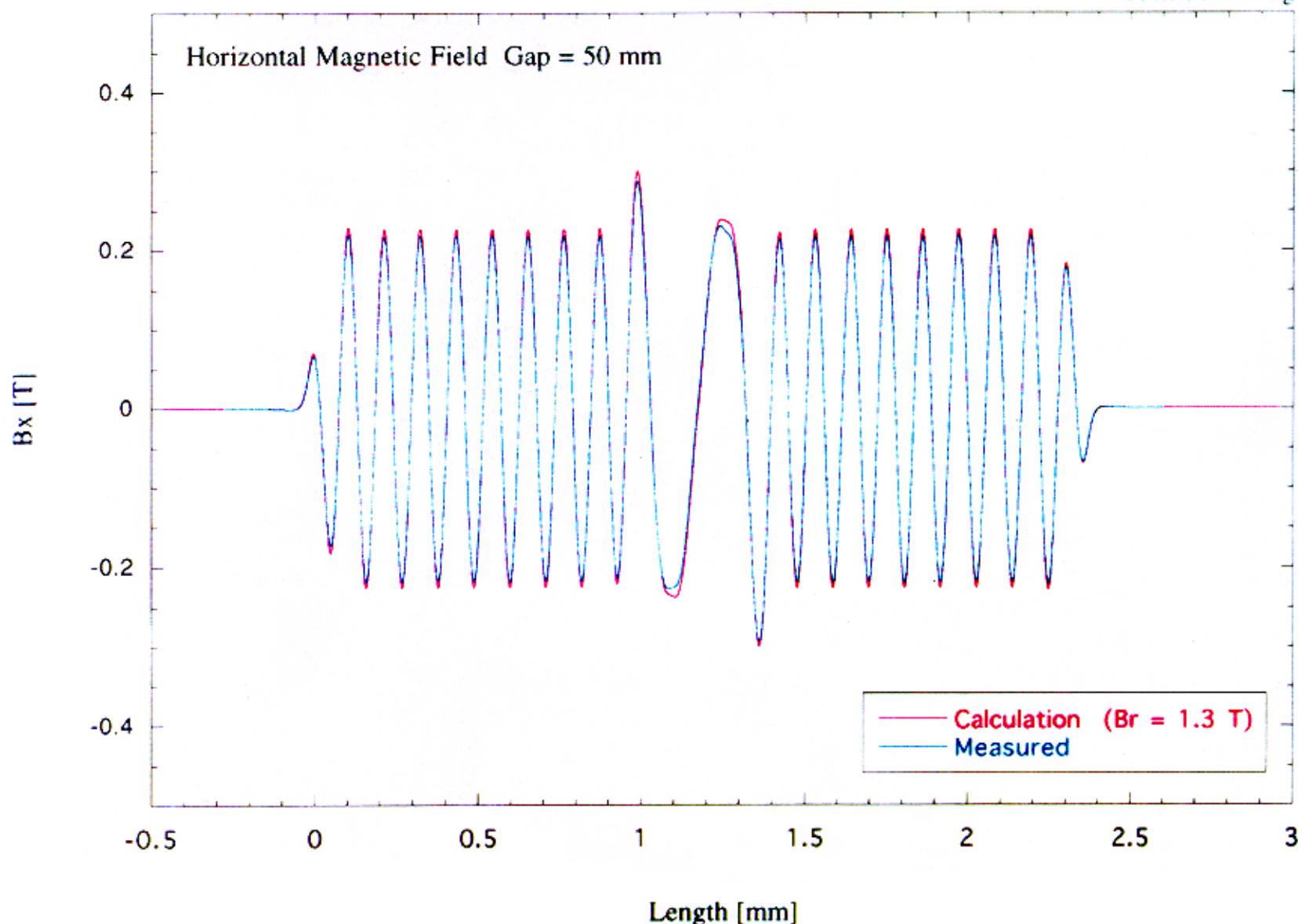
Helical Mode A

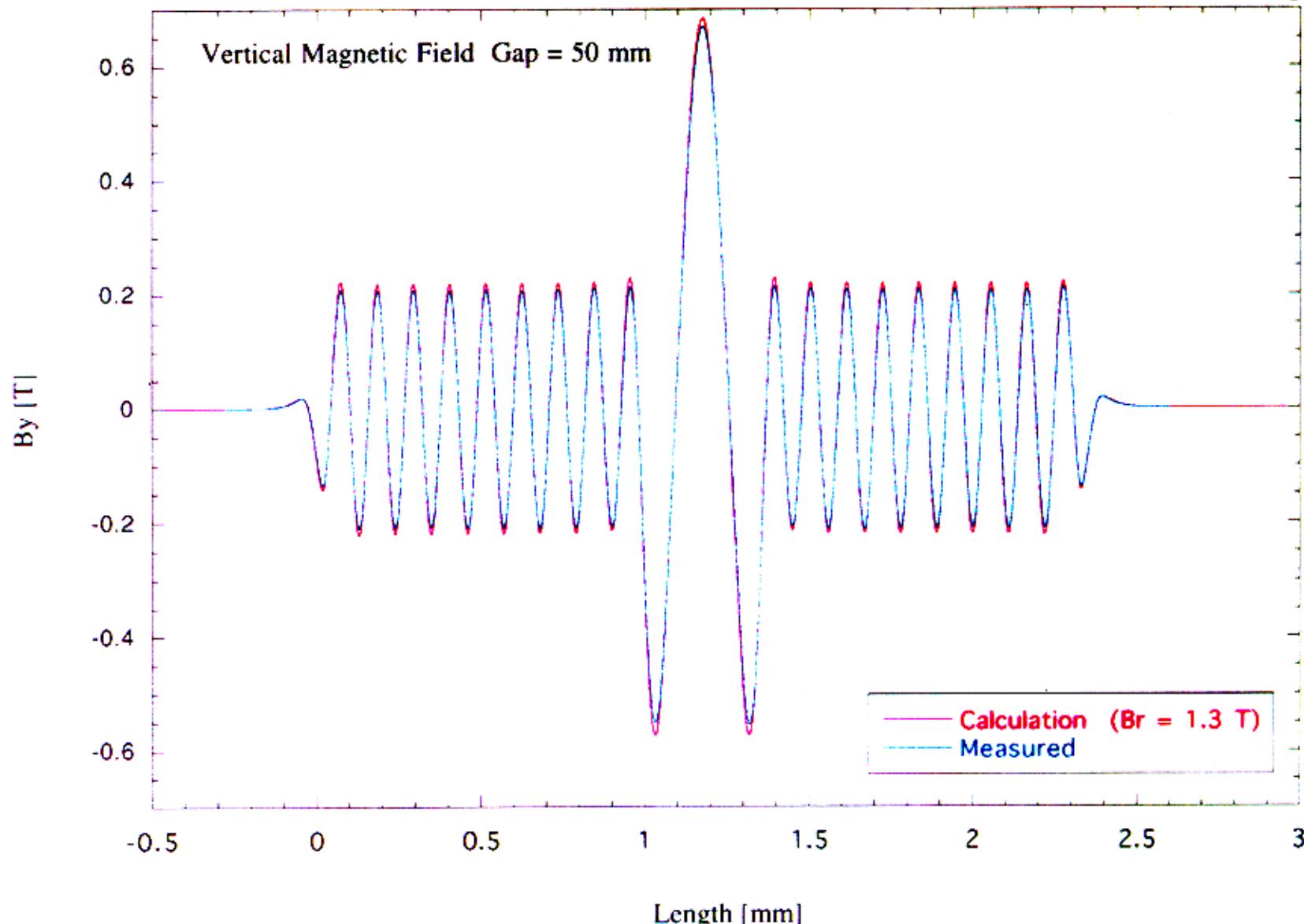
Planar Mode

Helical Mode B









# ISSUES OF UNDULATORS FOR (LOW ENERGY) STORAGE RINGS

## 1. Additional Focusing Power ( $B_z$ on off-axis)

0-th order Quadrupole       $k l = \frac{B_o^2 \lambda_p N_p}{2 (B\beta)^2} [T/m]$

Very important effect for low energy machines.

Long undulator is also critical issue for even high energy machines.

## 2. Multipole Focusing Power (Multipole fields in Curvilinear system)

Inhomogeneous field gives complicate multipoles on the beam trajectory.

## 3. Errors

Magnetic field measurements are always correct ?

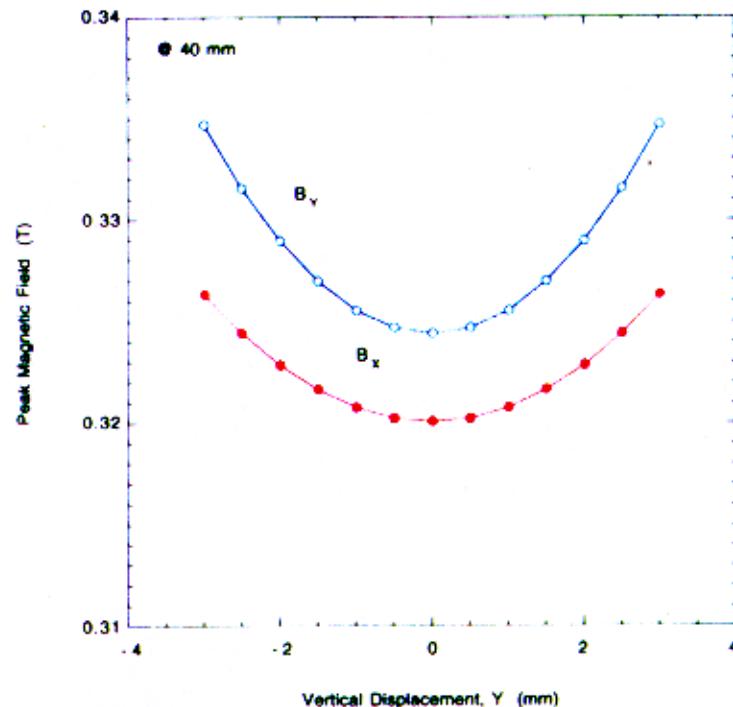
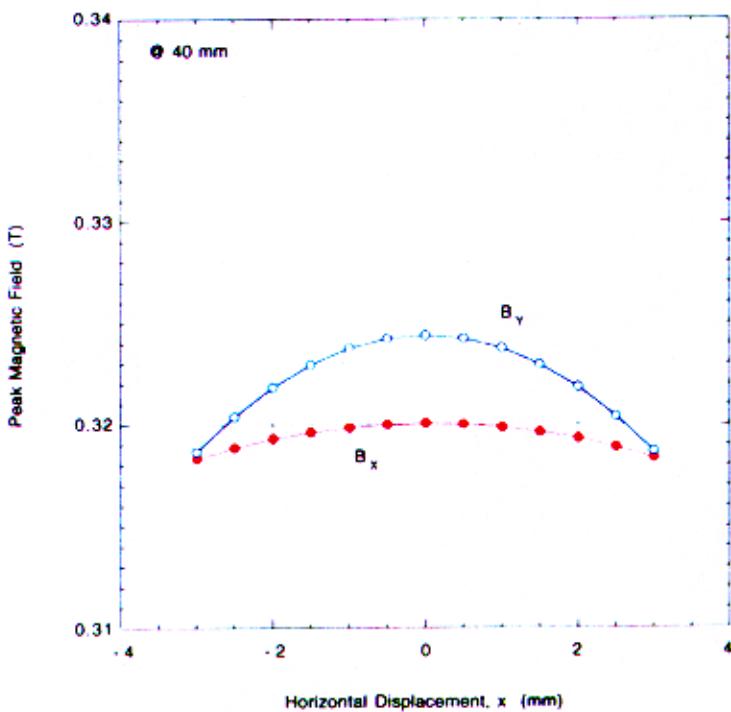
How we correct COD ?

COD correction is not equivalent to correction of beam trajectory in the undulator.

## Characteristics of Magnetic Fields in UNKO-3

Very narrow uniform region.

Same displacement dependences for inhomogeneous  $B_x$  and  $B_y$  fields



To satisfy eq. (10),

$$\frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2} = (-k_x^2 + k_y^2) \cos(k_x x) \cosh(k_y y) \quad \text{and} \quad \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} = (-j_x^2 + j_y^2) \cos(j_x x) \cosh(j_y y) \quad (12)$$

then conditions

$$k_p^2 = -k_x^2 + k_y^2 \quad \text{and} \quad k_p^2 = -j_x^2 + j_y^2 \quad (13)$$

are required.

The longitudinal field can be obtained from  $\frac{\partial B_z}{\partial z} = -\frac{\partial B_x}{\partial x} - \frac{\partial B_y}{\partial y}$

Finally

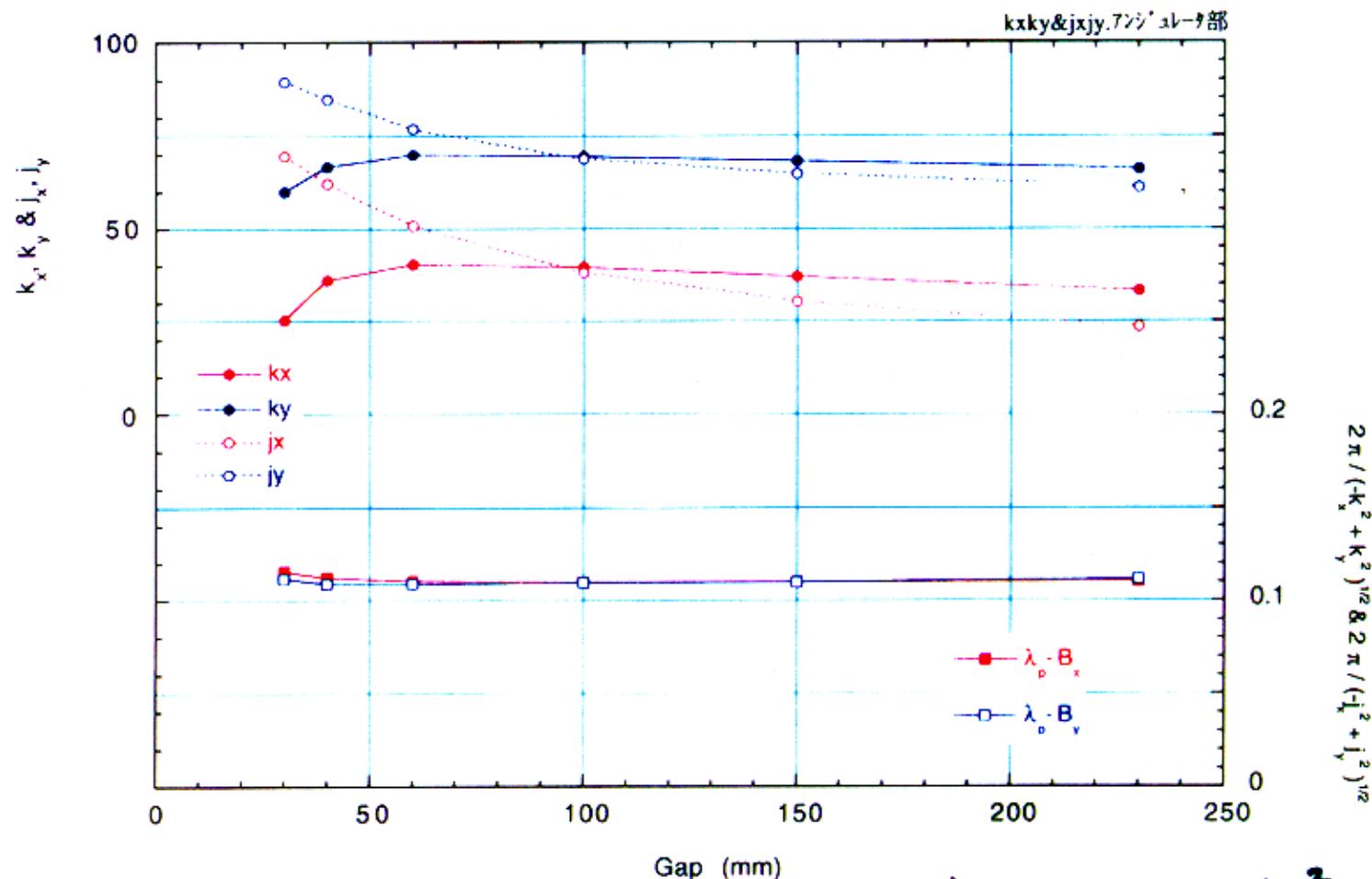
$$B_x = B_x^0 \cos(k_x x) \cosh(k_y y) \sin(k_p z)$$

$$B_y = B_y^0 \cos(j_y x) \cosh(j_y y) \cos(k_p z)$$

$$B_z = -B_x^0 \frac{k_x}{k_p} \sin(k_x x) \cosh(k_y y) \cos(k_p z) - B_y^0 \frac{j_y}{k_p} \cos(j_y x) \sinh(j_y y) \sin(k_p z)$$

$$k_p^2 = -k_x^2 + k_y^2 = -j_x^2 + j_y^2$$

## Inhomogenous parameters ( $k_x$ , $k_y$ , $j_x$ , $j_y$ ) deduced from magnetic field calculation



$$\lambda_p = 0.11 \text{ m} \quad k_p^2 = -k_x^2 + k_y^2 - j_x^2 + j_y^2$$

## UNDULATOR SECTION (per one period)

## Horizontal Plane

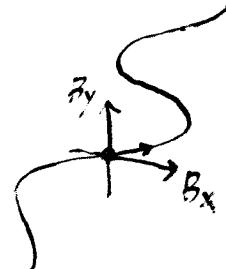
Quadrupole ( $kl$ )

$$\frac{\lambda_p}{2B\rho k_p^2} \left( B_x^{02} k_x^2 + B_y^{02} j_x^2 \right) + \frac{\lambda_p}{16B\rho^4 k_p^6} \left( B_x^{04} k_x^2 k_y^2 + 3B_x^{02} B_y^{02} j_x^2 j_x^2 \right)$$

defocus                                      may be very small

Skew-Q like ( $x y^2$ )

$$\frac{\lambda_p}{4B\rho k_p^2} \left( B_x^{02} k_x^2 k_y^2 + B_y^{02} j_x^2 j_y^2 \right)$$



## Vertical Plane

Quadrupole ( $kl$ )

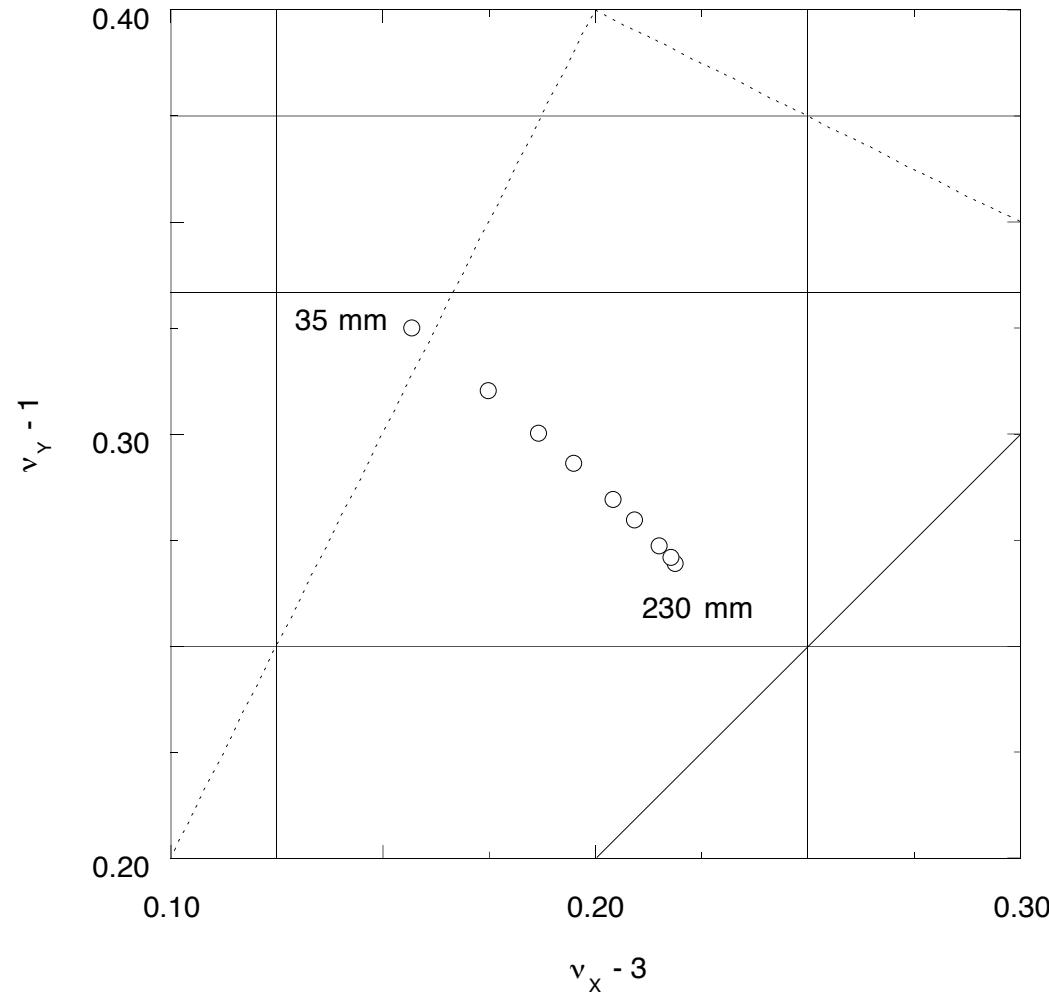
$$- \frac{\lambda_p}{2B\rho k_p^2} \left( B_x^{02} k_y^2 + B_y^{02} j_y^2 \right) + \frac{\lambda_p}{16B\rho^4 k_p^6} \left( B_y^{04} j_x^2 j_y^2 + 3B_x^{02} B_y^{02} k_x^2 k_x^2 \right)$$

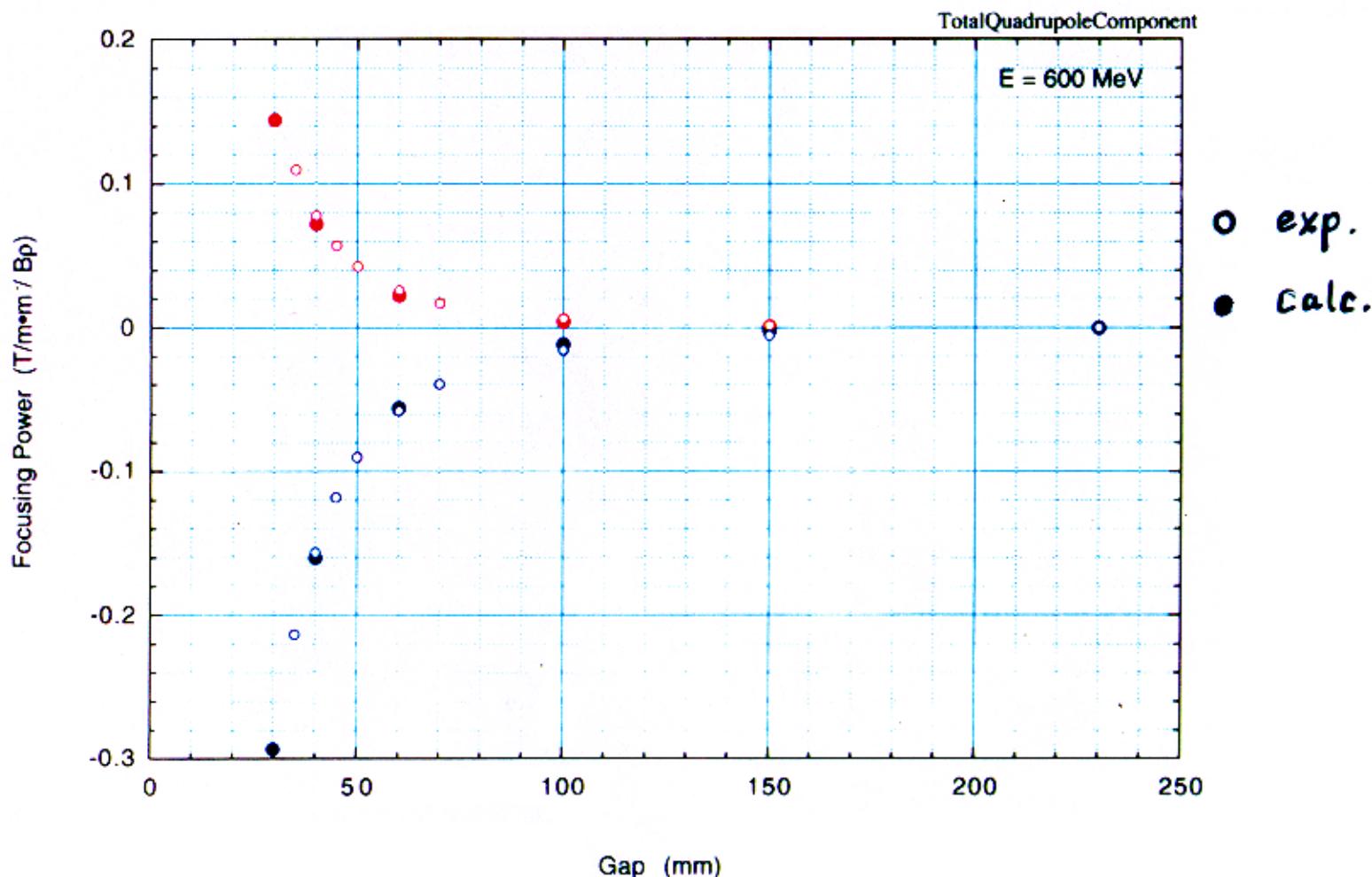
focus                                      may be very small

Skew-Q like ( $x y^2$ )

$$\frac{\lambda_p}{4B\rho k_p^2} \left( B_x^{02} k_x^2 k_y^2 + B_y^{02} j_x^2 j_y^2 \right)$$

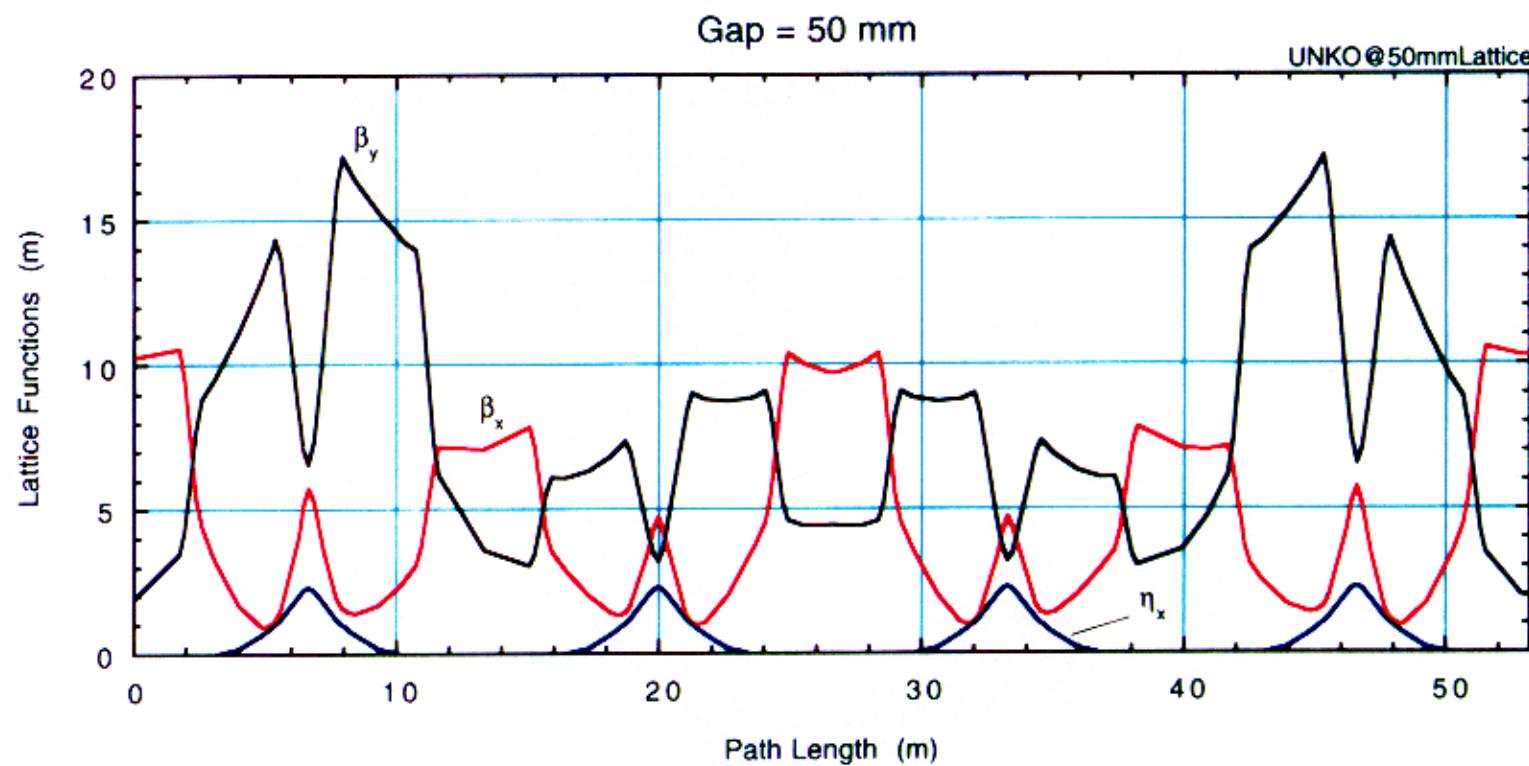
## Tune shift due to UNKO-3



**Quadrupole strength (Open circles : experiment)**

## Distortion of lattice function due to Q-strength of UNKO-3

Number of Quadrupoles to correct

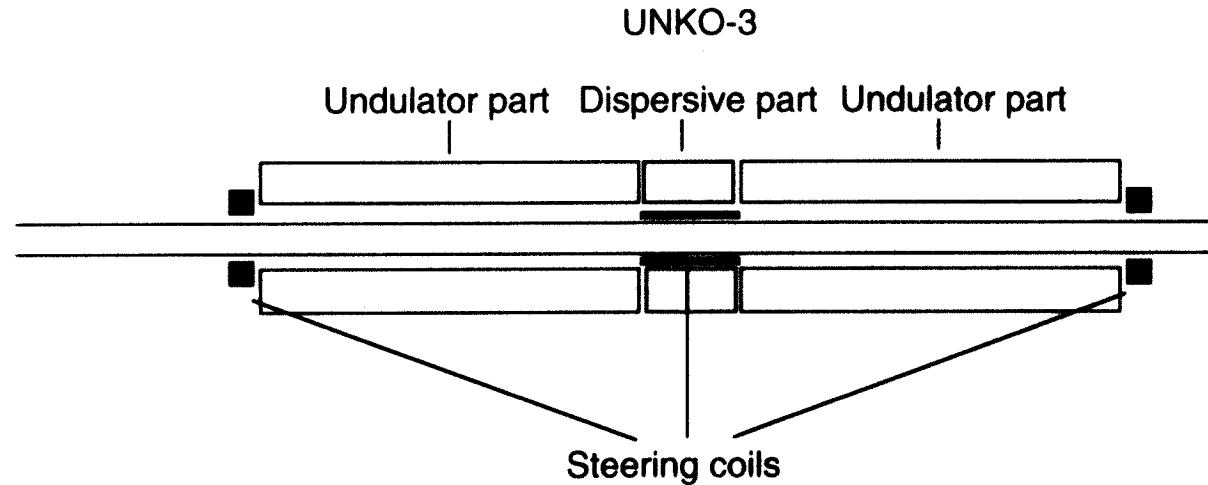
symmetry  
phase advance4  
+ 2

No solution gap < 45 mm

→ Quadrupole correction

## DIPOLE ERRORS

Three possible correction points



Dipole error source is devided into three positions !

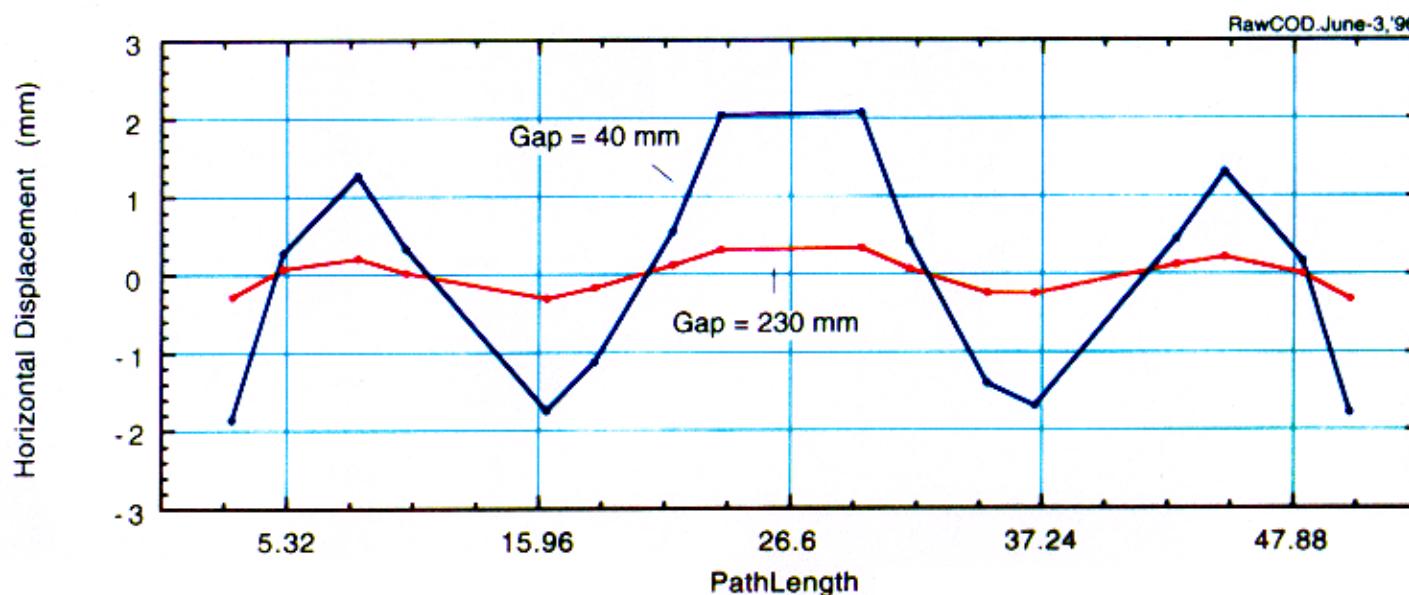
COD due to dipole kick can be written as

$$COD(s) = \frac{\theta_{kick}}{2} \sqrt{\beta(s) \beta(s_{kick})} \frac{\cos v \left[ \pi - |\phi(s) - \phi(s_{kick})| \right]}{\sin \pi v}$$

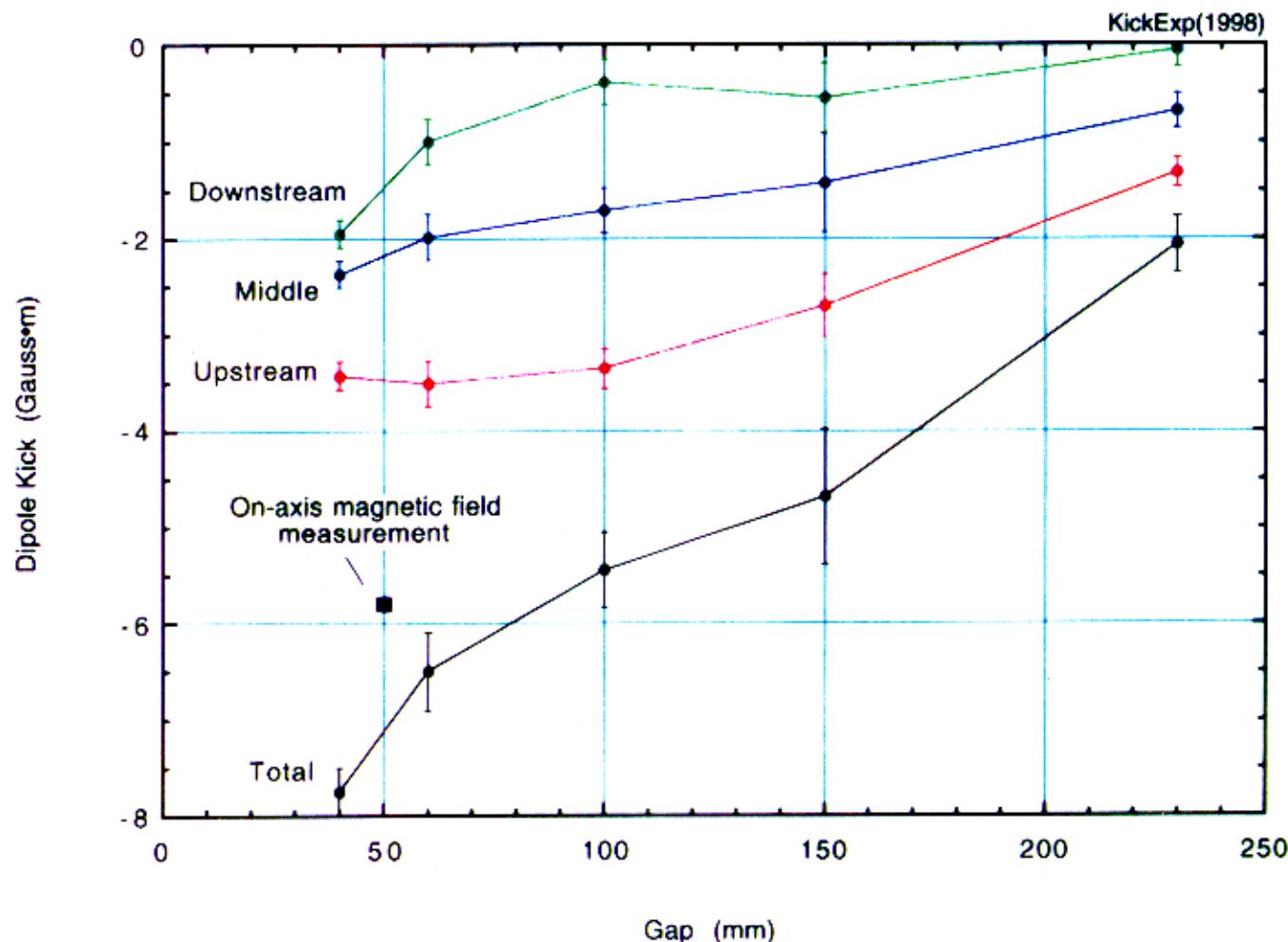
## COD Phase analysis with 3 kick sources

$$COD(s) = \theta_{kick}^1 u'(s_{kick}^1) + \theta_{kick}^2 u'(s_{kick}^2) + \theta_{kick}^3 u'(s_{kick}^3) \quad u'(s_{kick}^n) = \frac{1}{2} \sqrt{\beta(s) \beta(s_{kick}^n)} \frac{\cos v \left[ \pi - \left| \phi(s) - \phi(s_{kick}^n) \right| \right]}{\sin \pi v}$$

Using 16-BPM data for Least Square Fitting to derive  $\theta_{kick}^n$  and  $u'(s_{kick}^n)$  is not only able to be calculated from Lattice Function but also can be measured by using well-calibrated steerings.



## Horizontal Dipole Kicks Derived from COD Phase Analysis

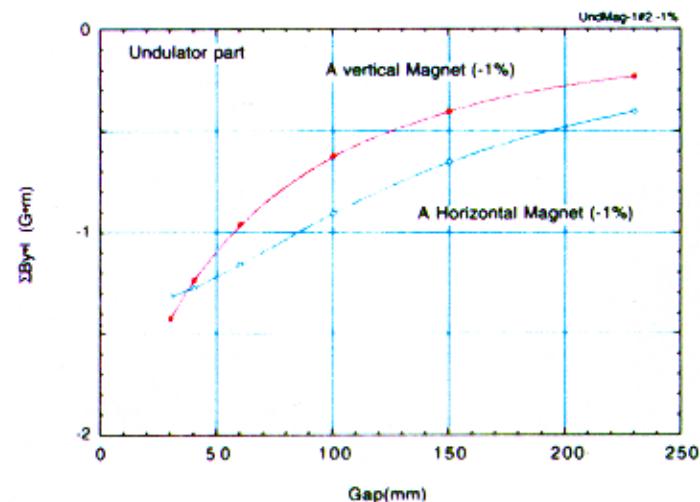


## How do we know "Error Sources" ?

Horizontal Magnetic Field  $\Rightarrow$  Composed field of Vertical and Horizontal Magnets

$$B_R = B_R^0 + \Delta B_R$$

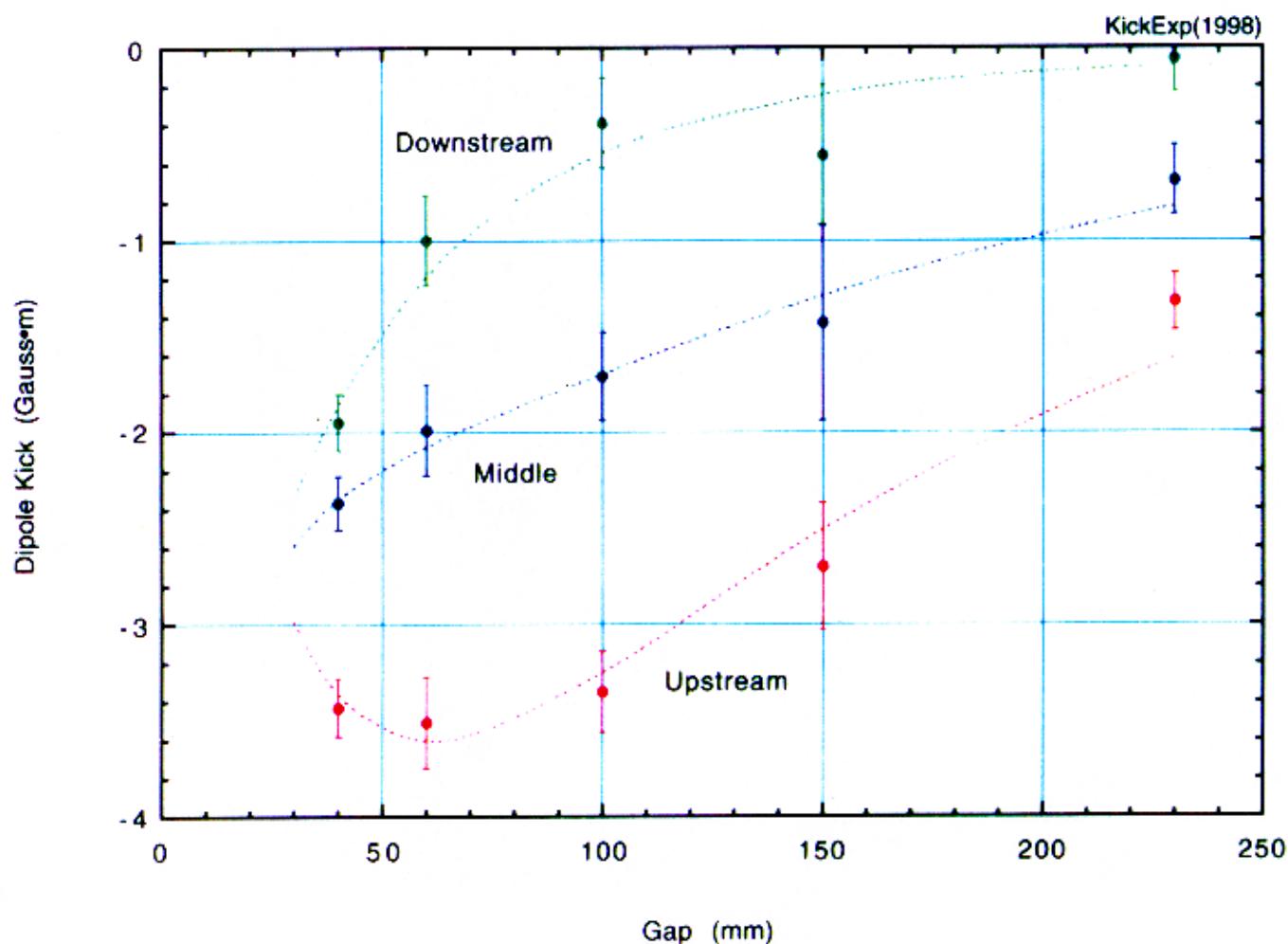
$$B_R = B_R^0 + \Delta B_R$$



Fitted results ( $\Delta B_R / B_R$ )

	Upstream	Middle	Downstream
Vertical Magnet	+ 3.3 %	+ 0.8 %	- 3.0 %
Horizontal Magnet	- 5.9 %	- 1.1 %	+ 1.5 %

## Analysis of 3 error sources

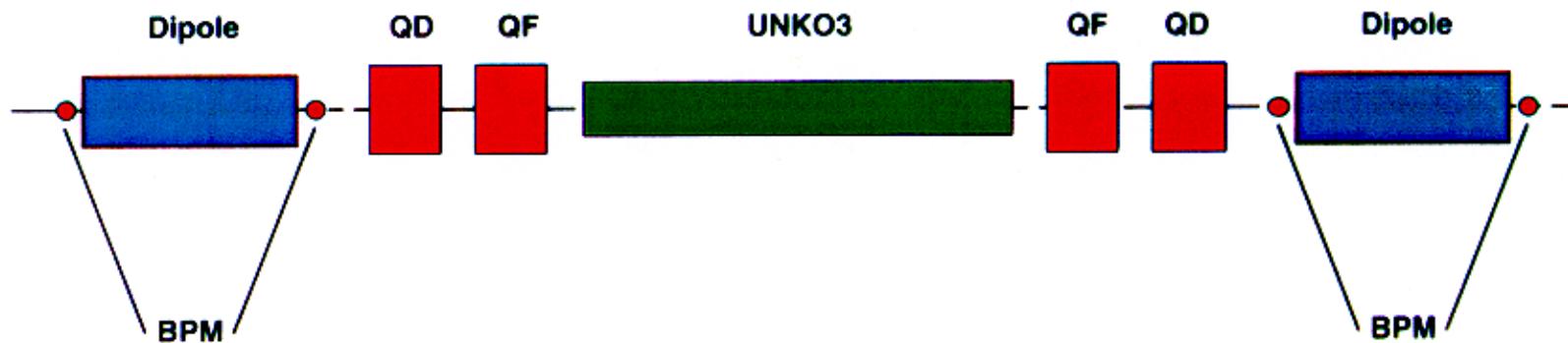


## BEAM-BASED ALIGNMENT OF QUADRUPOLES AND UNDULATOR

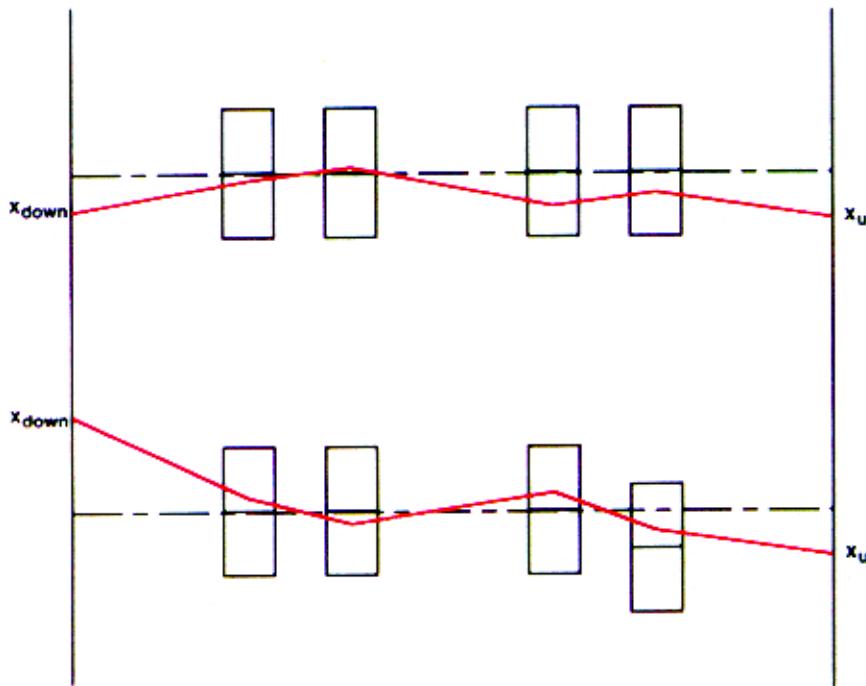
UNKO-3 : Very strong quadrupole strength for both horizontal and vertical directions !

Beam off-axis of Q-magnetic center : Quadrupole kick in the undulator  
Beam on-axis : Straight trajectory

There are not enough number of BPMs on the UVSOR ! (not common problem)



Before the undulator is put on the storage ring, we should know **misalignment of Quadrupoles !!!**



If there is no misalignment,

$$\vec{x}_{down} = \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 \tilde{Q}_3 \tilde{L}_3 \tilde{Q}_2 \tilde{L}_2 \tilde{Q}_1 \tilde{L}_1 \vec{x}_{up}$$

If a Q-magnet is misaligned

$$\vec{x}_{down} = \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 \tilde{Q}_3 \tilde{L}_3 \tilde{Q}_2 \tilde{L}_2 \tilde{Q}_1 \tilde{L}_1 \vec{x}_{up} + \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 \tilde{Q}_3 \tilde{L}_3 \tilde{Q}_2 \tilde{L}_2 \vec{K}_1$$

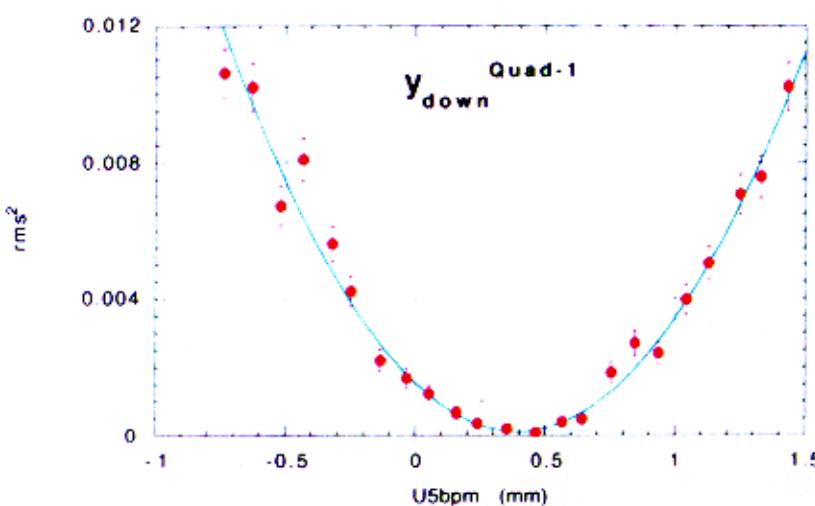
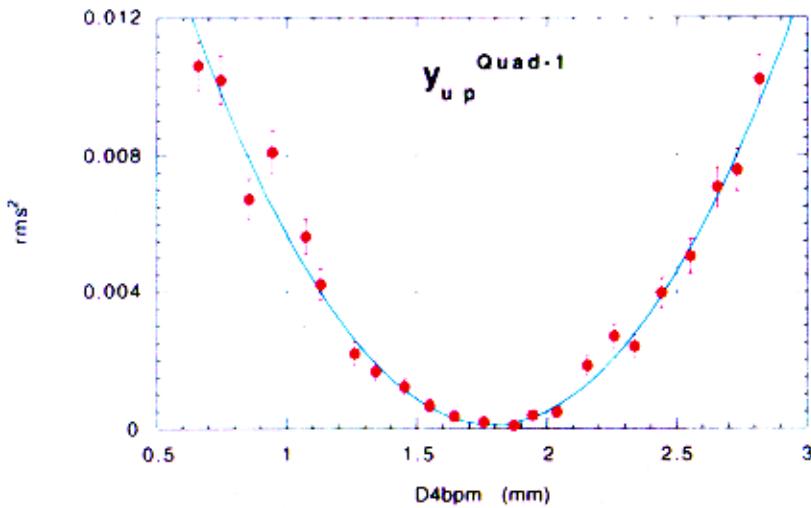
Taking all Q-misalignments into account,

$$\vec{x}_{down} = \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 \tilde{Q}_3 \tilde{L}_3 \tilde{Q}_2 \tilde{L}_2 \tilde{Q}_1 \tilde{L}_1 \vec{x}_{up} + \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 \tilde{Q}_3 \tilde{L}_3 \tilde{Q}_2 \tilde{L}_2 \vec{K}_1 + \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 \tilde{Q}_3 \tilde{L}_3 \vec{K}_2 + \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 \vec{K}_3 + \tilde{L}_5 \vec{K}_4$$

or

$$\begin{aligned} \vec{x}_{down} = & \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 \tilde{Q}_3 \tilde{L}_3 \tilde{Q}_2 \tilde{L}_2 \tilde{Q}_1 \tilde{L}_1 \vec{x}_{up} + \left[ \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 \tilde{Q}_3 \tilde{L}_3 \tilde{Q}_2 \tilde{L}_2 (\tilde{Q}_1 - \tilde{e}) \right] \begin{pmatrix} -c_1 \\ 0 \end{pmatrix} \\ & + \left[ \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 \tilde{Q}_3 \tilde{L}_3 (\tilde{Q}_2 - \tilde{e}) \right] \begin{pmatrix} -c_2 \\ 0 \end{pmatrix} + \left[ \tilde{L}_5 \tilde{Q}_4 \tilde{L}_4 (\tilde{Q}_3 - \tilde{e}) \right] \begin{pmatrix} -c_3 \\ 0 \end{pmatrix} + \left[ \tilde{L}_5 (\tilde{Q}_4 - \tilde{e}) \right] \begin{pmatrix} -c_4 \\ 0 \end{pmatrix} \end{aligned}$$

$$\frac{\Delta k}{k} \approx 5\%$$



	Displacement (mm)	
	Horizontal	Vertical
Quad-1	- 0.71	+ 1.67
Quad-2	- 0.64	+ 1.31
Quad-3	- 0.71	+ 0.73
Quad-4	- 0.90	+ 0.42

The displacement is a distance from a line connected to the BPM centers.

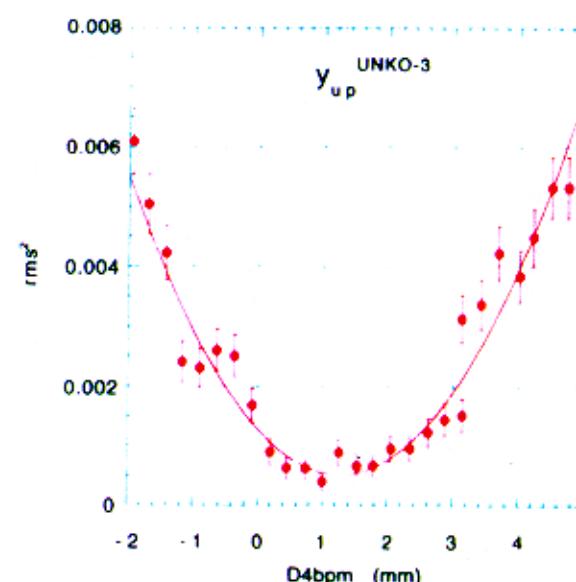
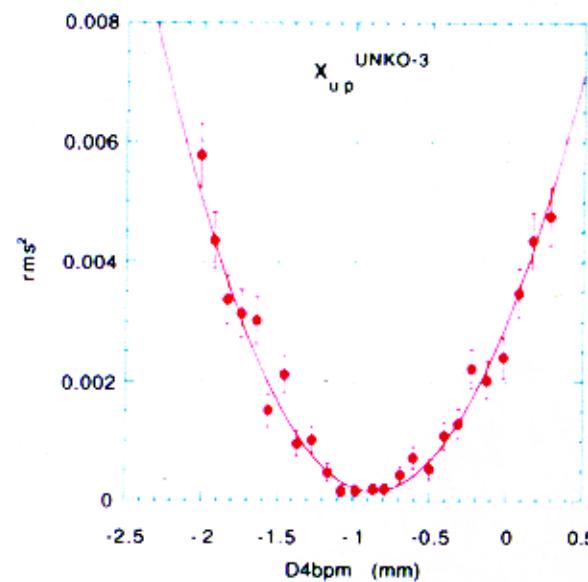
## Measurement of UNKO-3 Position

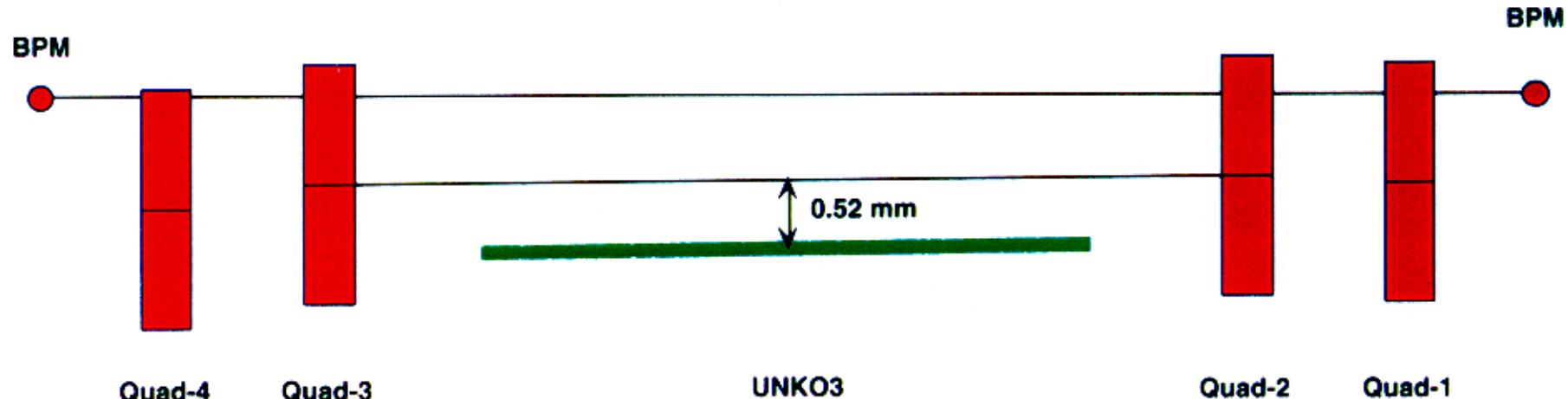
Definition of "UNKO-3's center" is a magnetic center of the Quadrupole strength !

Forget tilt !!

t

- Because the Q-magnets center are already known, the transfer matrix including UNKO-3's quadrupole strength is much more simple.
- By changing the gap, quadrupole strength of the UNKO-3 can be varied, then we can derive the absolute position of the magnetic center of UNKO-3.



**UNKO-3 Horizontal Position****UNKO-3 Vertical Position**